

## Homework Assignment #5

**Prob. 1 Leapfrog Filter.** Based on a third-order passive RLC Butterworth LP filter with a nominal cut-off frequency of 945 Hz.

- (a) Obtain corresponding RLC prototype
- (b) Write the state-variable equations describing the RLC
- (c) Implement the active version using a block diagram approach and an active-RC or an OTA-C implementation.

**Prob. 2 SC Biquad Design** based on the several biquads shown in power point notes:

- (a) Find the transfer function for Circuit 1 from notes (hint: use the corresponding block diagram and Mason's Rule).
- (b) Assuming that the design equations are (where K is in v/v):

$$|K| = \frac{a_5}{1 + a_8} \quad (w_o T)^2 = \frac{a_2 a_7}{1 + a_8} \quad Q = \frac{\sqrt{a_2 a_7 (1 + a_8)}}{a_8}$$

Design a circuit (capacitor values) with the following specifications:

$$f_c = 50\text{KHz}, f_o = 697 \text{ Hz}, A_{v\text{max}} = 1 \text{ v/v for all internal nodes at } f_o, \text{ and } Q = 25$$

- (c) Simulate the filter using SWITCAP (or other SC simulator). Provide its frequency plot; magnitude and delay.
- (d) Repeat (a) – (c) for Circuit 2. The design equations are (where K is in dB):

$$\frac{C_2}{C_{F1}} = \frac{C_3}{C_{F2}} \cong 2p f_o T \quad \frac{C_2 C_4}{C_{F1} C_{F2}} = \frac{2p f_o T}{Q} \quad \frac{C_1 C_2}{C_{F1} C_{F2}} = |K|$$

- (e) Compare the total capacitance area of both circuits. Propose a modified structure of Circuit 2 that reduces the capacitance area (hint: use a “Qunting Integrator” and a Offset and Gain Compensated Integrator).

EXTRA CREDIT: (A must for Graduate Students)

Repeat 2(b) for  $f_c = 6\text{KHz}$ , compare total capacitance area for all the cases. Discuss performance differences of the different designs and their strengths and weaknesses